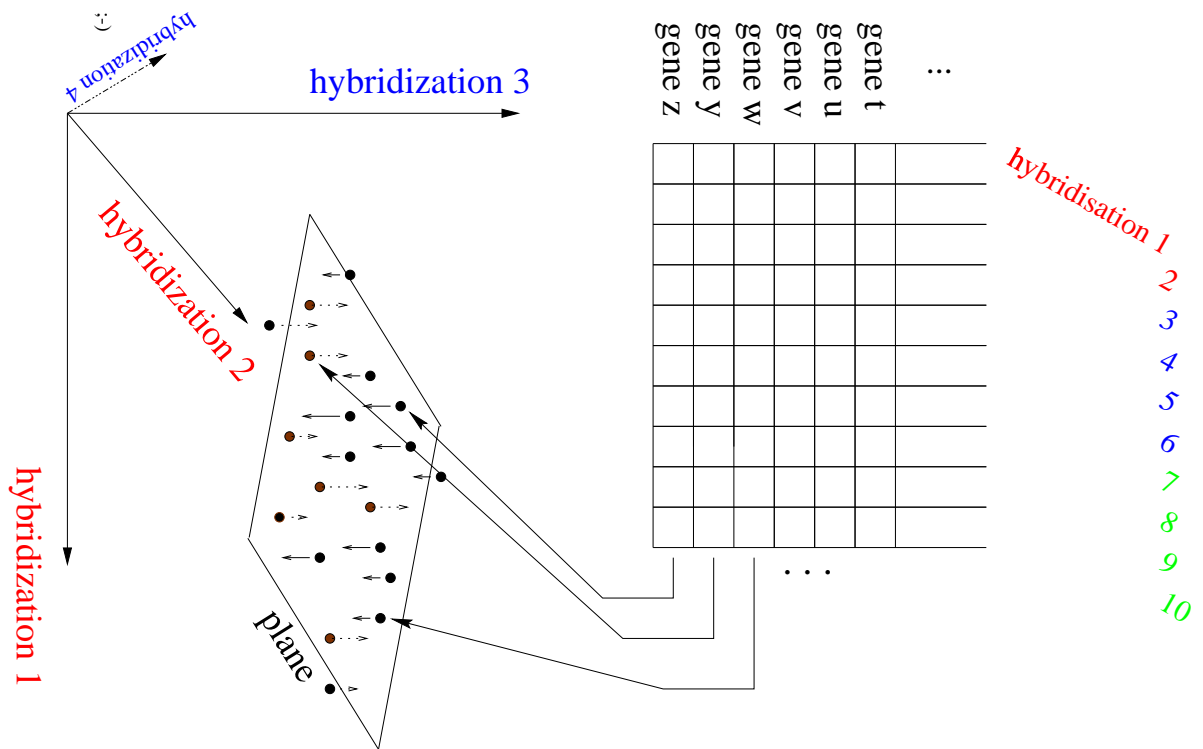
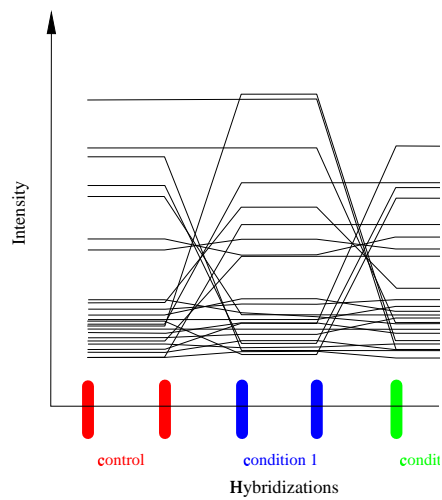


The m columns of a table of n genes \times m hybridizations are represented in n -dimensional gene space (three dimensions are shown). n ranges from a few hundred to tenths of thousands. Most microarrays comprise several thousand elements. A plane is selected such that the distance of the hybridization vectors to the plane is minimal, thus conserving point-to-point distances among these vector points as well as possible.

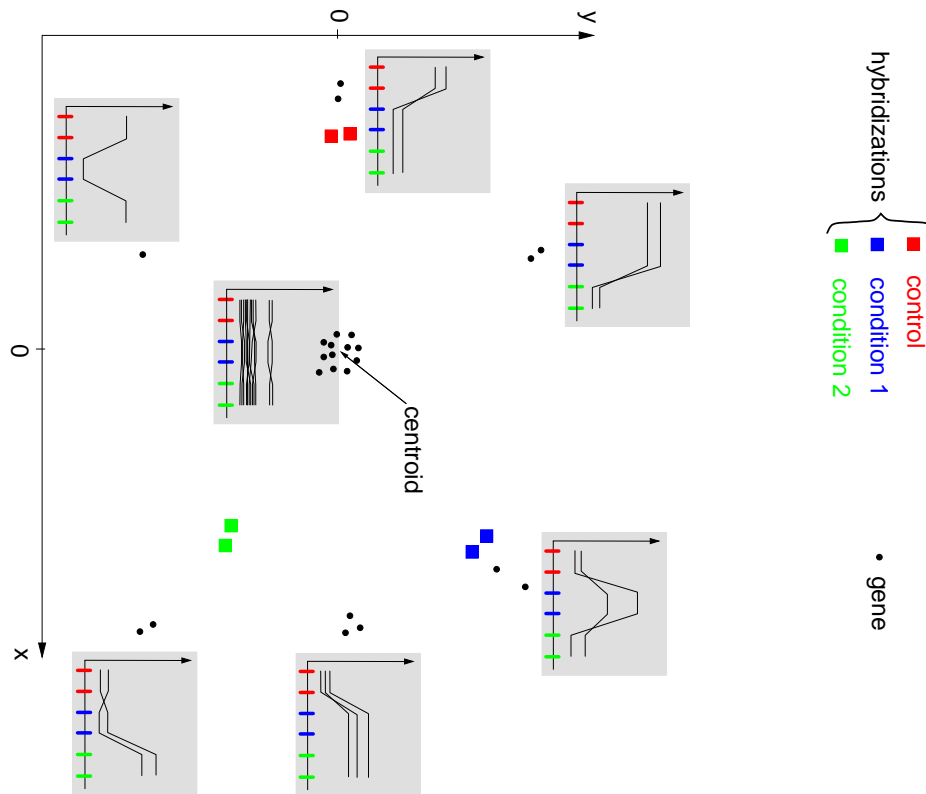


Vice versa, one can regard the gene vectors in hybridization-dimensional space, projecting the genes as done above for the hybridizations.



To look into the interpretability of such a plot, let me introduce a constructed (virtual) data

example. It resembles real data in that the majority of the genes is lowly or not transcribed to a measurable amount. It comprises only 24 genes and differs from the real world in perfect reproducibility among the two hybridizations of each experimental condition.

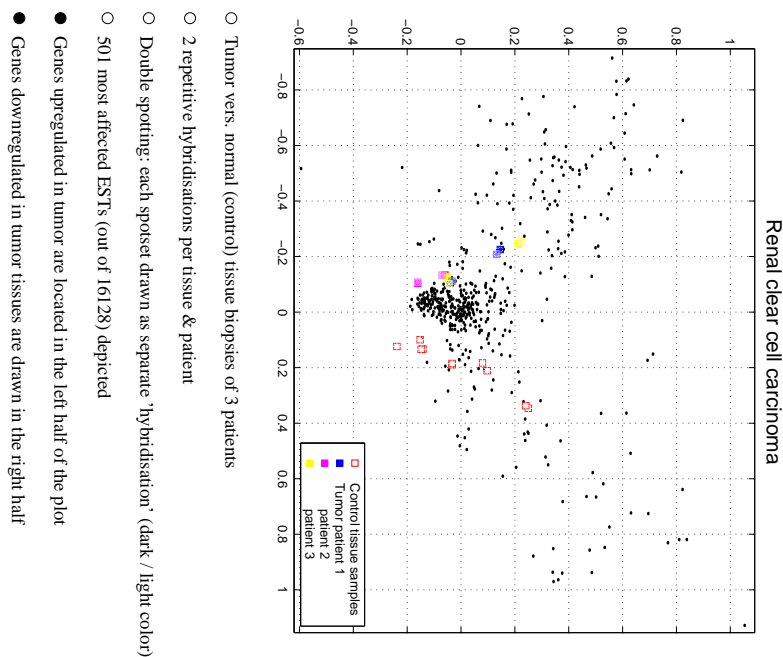


This is the expected output, demonstrating the properties of such projections more clearly than possible by showing a single plot of real data. Gene-clusters are shown together with the according gene profiles. The abscissa represents the first, the ordinate the second principal axis. Both axes are dimensionless. The following properties of such a plot are useful for its interpretation.

- Hybridizations showing high similarity in expression profile, for example because they belong to the same experimental condition, have a short distance in the 24-dimensional gene space, and therefore they will be neighbors in the projection as well.
- Genes with high intensities in a condition are located in the direction of this condition. The two genes located in the direction of the blue condition (upper right corner) are both upregulated particularly in the blue condition.
- Genes particularly downregulated under this condition are located at the opposite side of the centroid. One can regard this gene (lower left corner) as being downregulated in

the blue condition. Another valid interpretation is, that it is located in the direction of the bisection line between the red and the green condition because it is equally abundant in these two conditions.

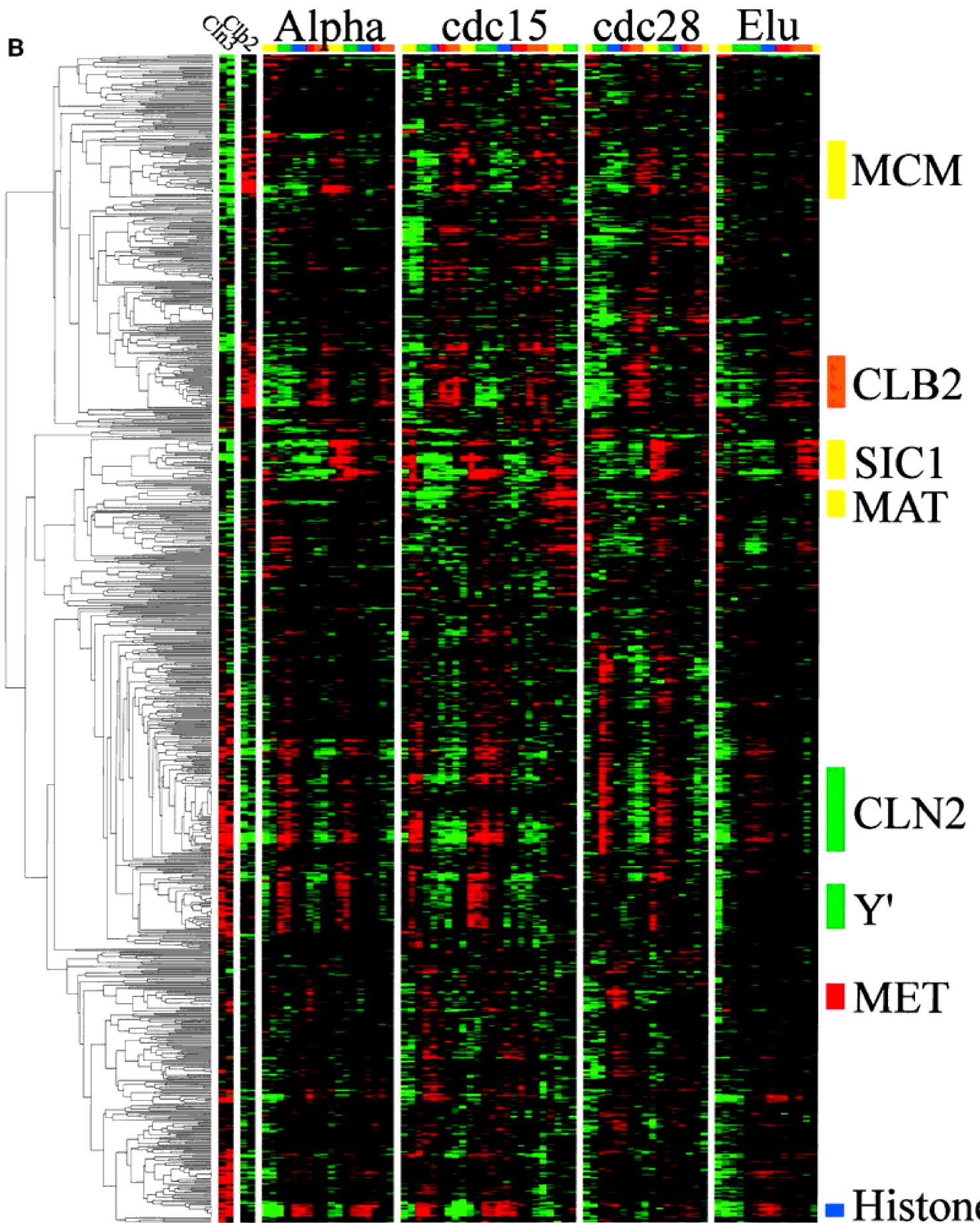
- All genes with unchanged expression, or those not expressed to a measurable amount in any of the conditions under study are located near the centroid. For experiments with comprehensive or complete gene sets, i.e. sets not particularly selected for high expression, the genes that are not detectable will be the majority. The CA plot will show a centric cloud of many genes lacking significantly changed expression throughout the experiment. The outer regions of the plot will contain the so-called ‘differential’ genes. Their distance to the centroid will reflect the significance of displaying differing expression from the ‘average’ ones in terms of χ^2 - statistics, which are placed at the center of the plot.

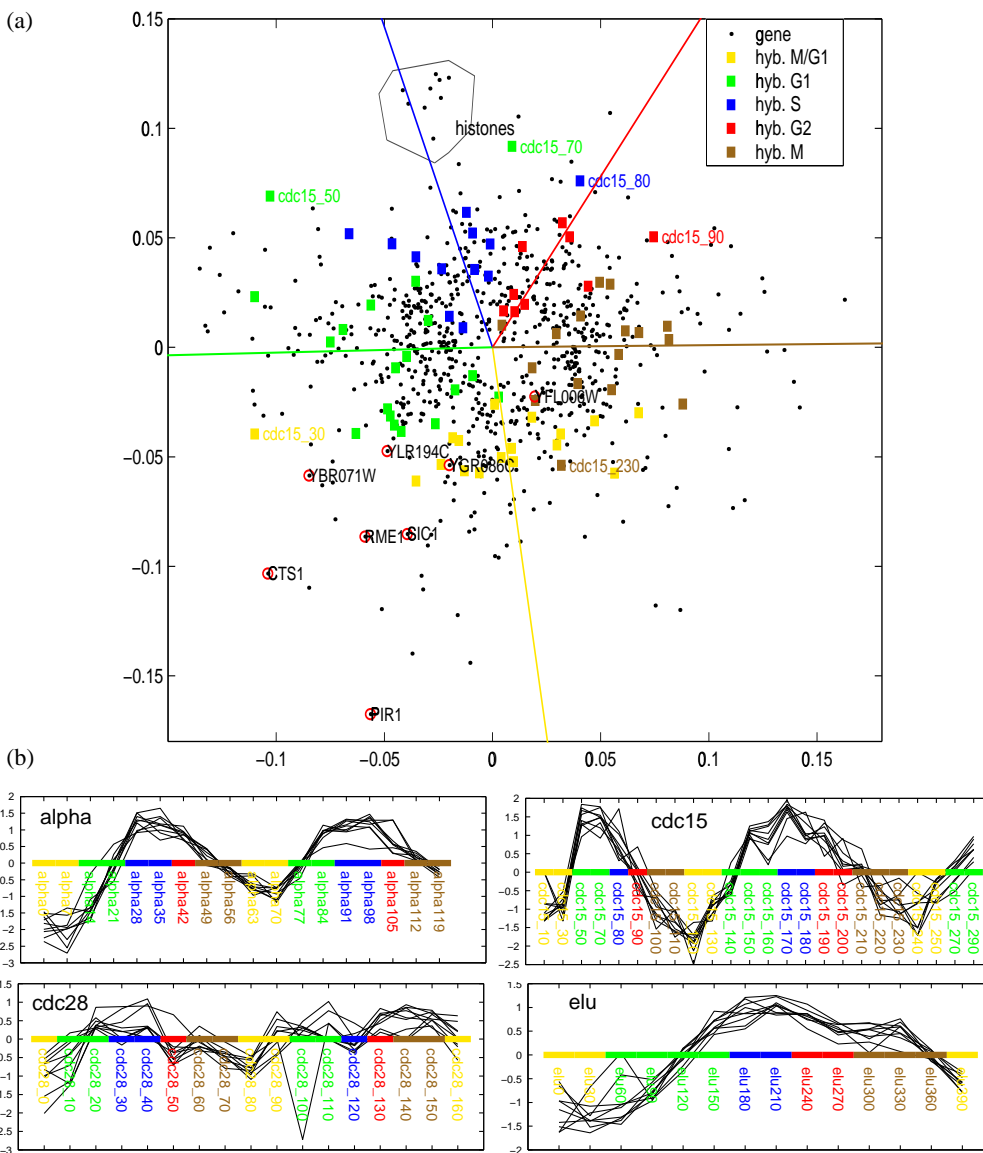


- Tumor vers. normal (control) tissue biopsies of 3 patients
- 2 repetitive hybridisations per tissue & patient
- Double spotting: each spotset drawn as separate 'hybridisation' (dark / light color)
- 501 most affected ESTs (out of 16128) depicted
- Genes upregulated in tumor are located in the left half of the plot
- Genes downregulated in tumor tissues are drawn in the right half

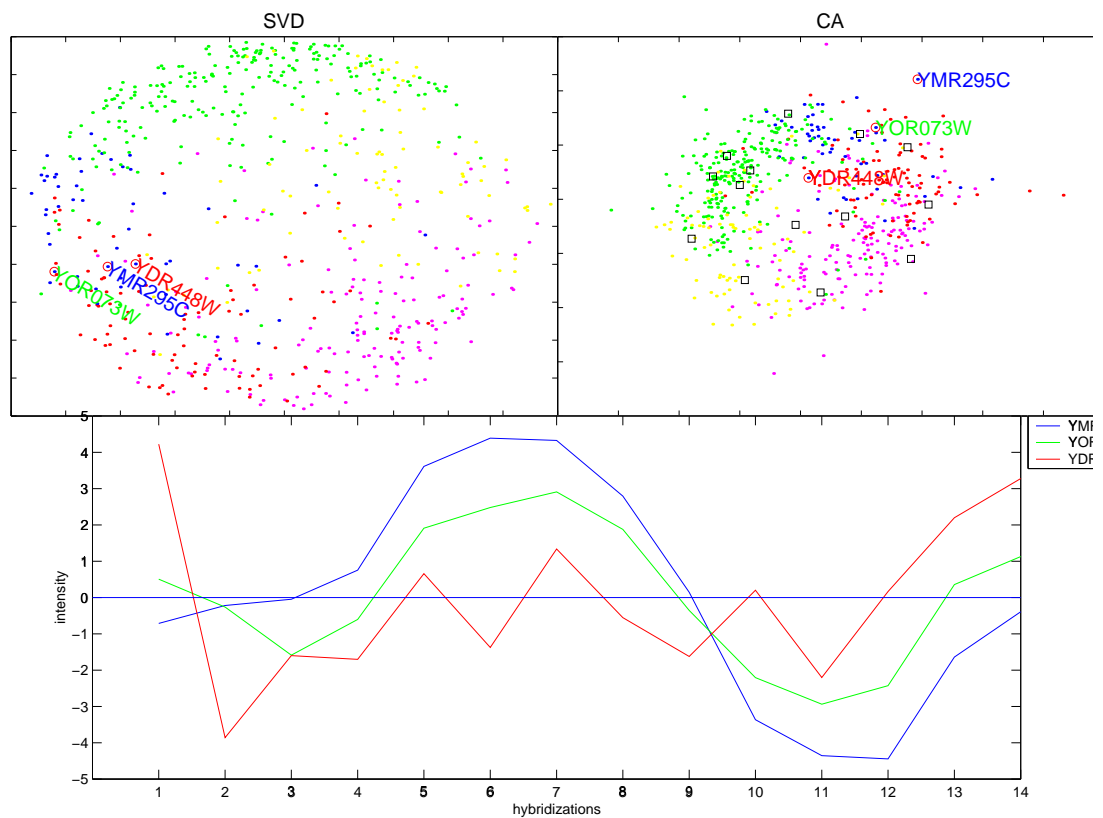
Now knowing at least roughly how to interpret such a plot, let's have a look on a simple real data example. Biopsies of both tumor tissue - the tumors being renal clear cell carcinoma - and normal tissue of the same patient (as a control) have been sampled and hybridised, imaged, normalized, quality filtered and projected.

The tumor tissues on the left half of the plot - tagged by three colors for three different patients - are separated from the normal tissue samples on the right. And all the genes upregulated in the tumor are located on the left side, all those downregulated in the tumor we find in the right half of the plot.



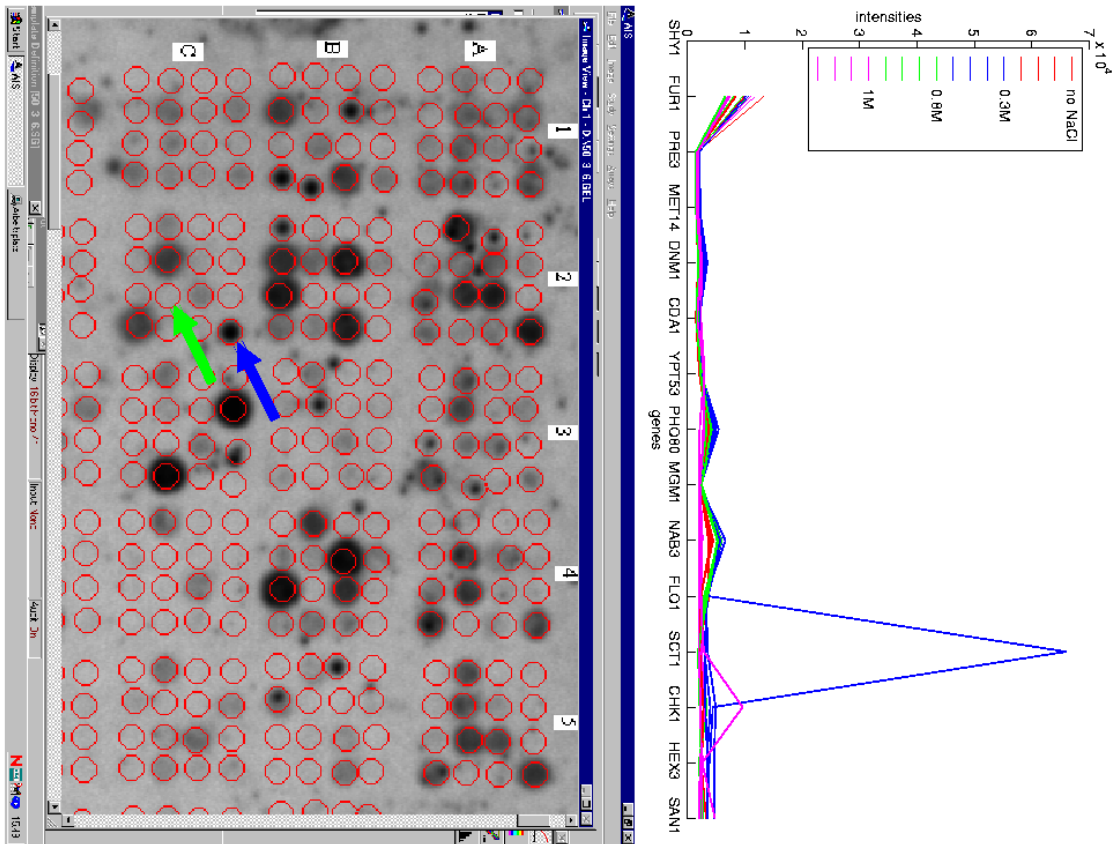


The planar embedding (of exactly the same data) produced by CA shows the hybridizations clearly separated according to their cell cycle phase. They are arranged in circular order of correct sequence. The lines denoting the direction of the hybridization medians emphasize



Alter *et al.* (O. Alter, P. O. Brown, and D. Bostein. Singular value decomposition for genome-wide expression data processing and modeling. Proc. Natl. Acad. Sci. U.S.A., 97:10101-10106, 2000.) successfully applied singular value decomposition to the analysis of the same data set. In CA plots, the distance of a given gene from the centroid represents the strength of its association with a hybridization lying in the same direction and vice versa. A direct comparison with phase and radius in the visualization of Alter *et al.*² shows that this is not necessarily the case in the singular value decomposition alone.

²as given e.g. at http://genome-www.stanford.edu/SVD/PNAS/Datasets/Sort_Elutriation.txt



As shown above, it might be useful to visualize deviations of outlying measurements from the expected state. However, data sets frequently comprise severe outliers such as this one.

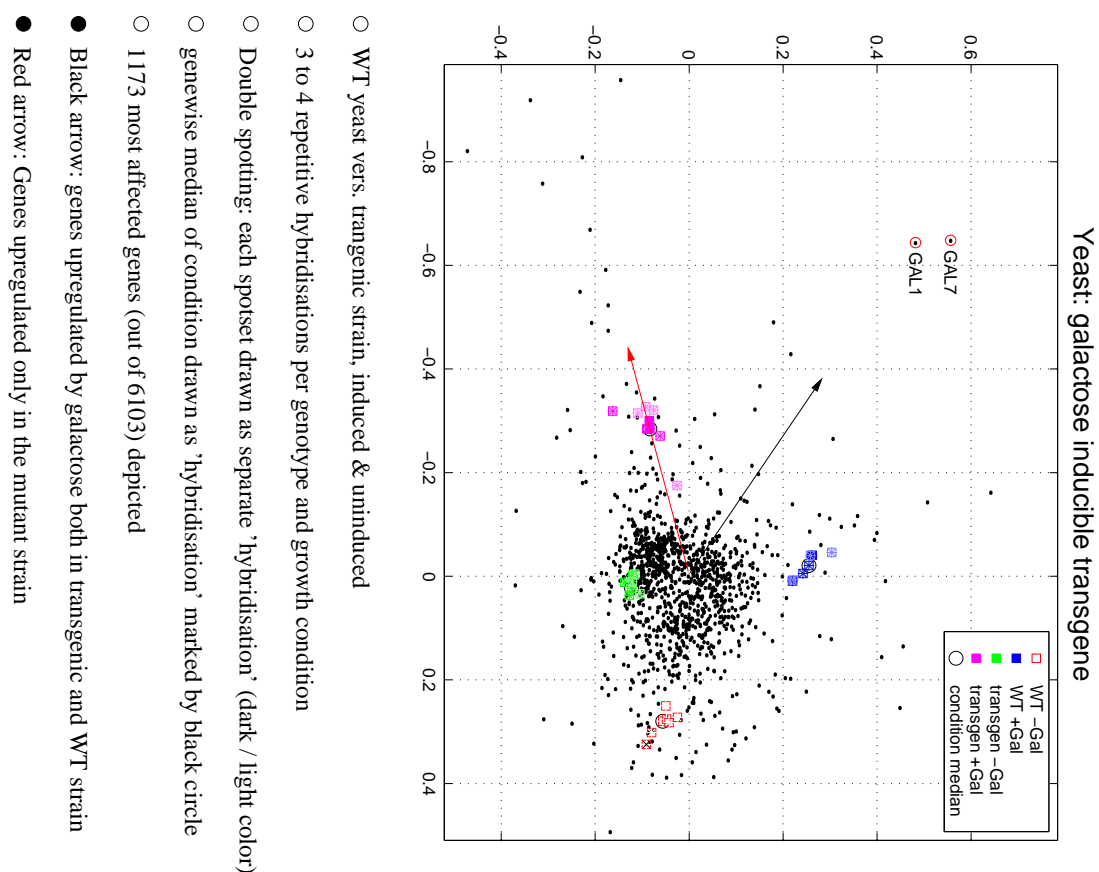
Wild type yeast was exposed to different concentrations of sodium chloride in the medium (see legend). Normalized transcription intensities of 14 genes are shown in a parallel coordinates plot, lines representing measurements and being color coded according to their particular experimental condition. The plot presents a typical subset of genes, representative with regard to the high number of genes not expressed to a measurable amount. Whereas the different conditions are reproducibly measured for most genes, SCT1 shows one far outlying signal for 0.3M NaCl (blue), which in this case is due to agglutinated label. In the corresponding image (below), the bright dots of unspecifically bound label are common to radioactively labeled targets, whereas the most severe outliers among multichannel data are frequently caused by highly fluorescent dust (not shown). The ordinate shows arbitrary (machine dependent) intensity units.

For this reason, a thorough preprocessing is essential. Different normalization algorithms are applied to single and multichannel data for the different meaning of the particular raw intensities. Intensity-, ratio-, and reproducibility filters are applied to extract genes of marked

expression for both types of data.

Genes with generally low reproducibility for most of the conditions under study are filtered out by the reproducibility filter. However, with increasing numbers of conditions, discarding all genes with low reproducibility in one of the conditions will leave no gene undiscarded. The same is true for the intensity filter. It is therefore reasonable to use these filters to discard only genes with low abundance or low reproducibility (often coinciding) in all the conditions under study. Thus, outliers as shown above have to be handled by other measures. Otherwise, they would seriously interfere with CA analysis, which in contrast to other methods is not similarity-driven but aims at displaying variance. Any difference to the default state (expected value) such as an outlier, will be regarded as important for the projection. The larger the difference, the more distinctly the corresponding point will be plotted.

We prevent this by choosing the principal axes according to the condition medians only (HMS).

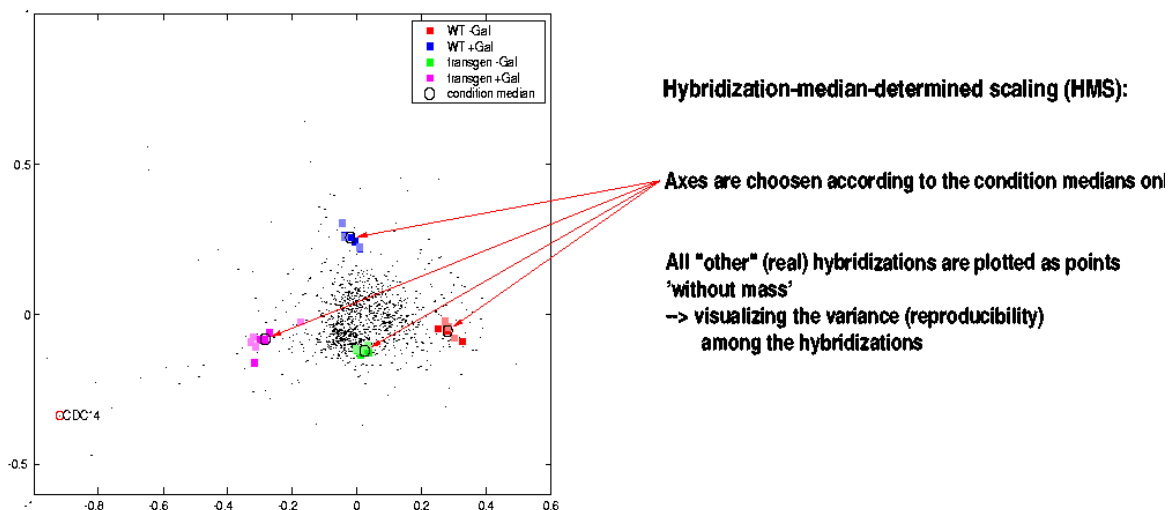


Let me first introduce a new data example. Here, a transgene was transfected into yeast cells under the control of a galactose inducible promoter:

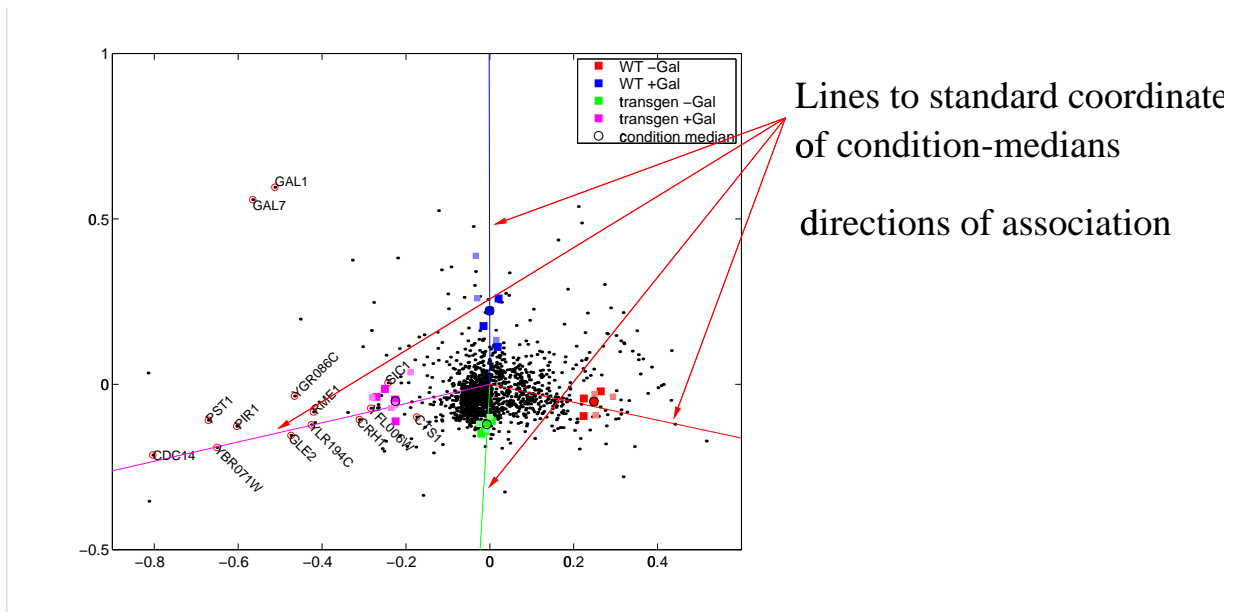
Red empty boxes are WT yeast without galactose in the medium, blue WT with galactose, green the transgenic strain without galactose and pink transgenic with galactose and here we

would expect the transgene to be induced and genes that follow the transgene. The aim was to separate those genes from all the genes which are upregulated by galactose in yeast anyway, that is: also in the WT strain.

The bisection line between WT and transgenic strain with galactose (black arrow) points to the genes induced by galactose both in the transgenic and in the WT strain. There we find genes like Gal 7 and Gal 1. The red arrow points to the genes upregulated specifically only in the transgenic strain - those are the genes the experimenter intended to look at with this experiment.

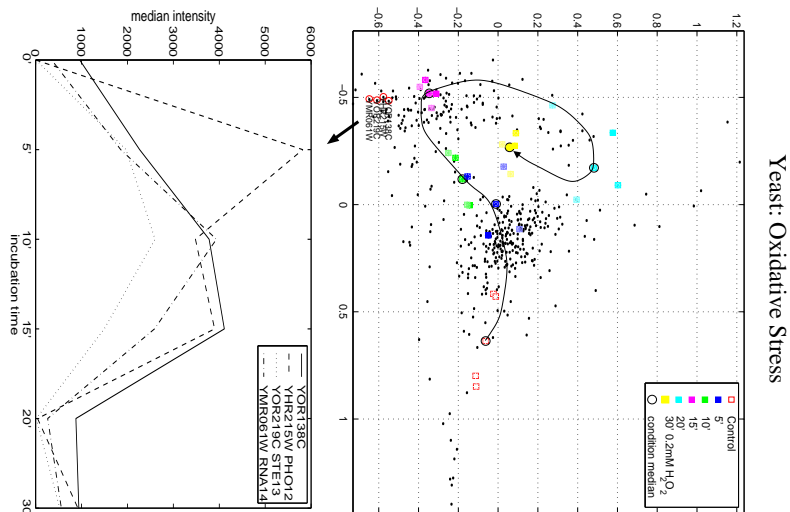
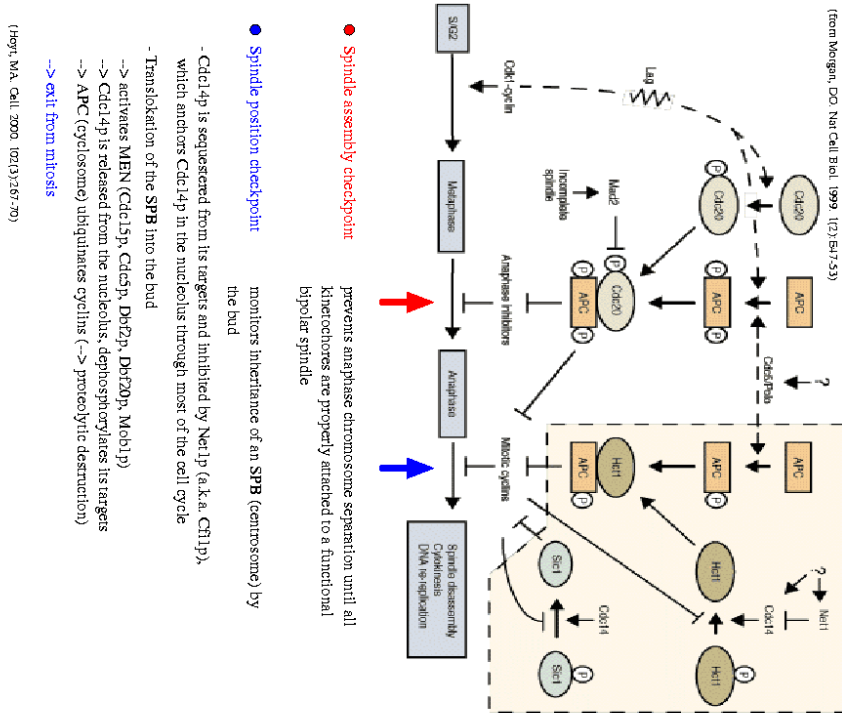


Typically, replicate hybridizations are performed for each condition under study leading to several values for one gene/condition pair. The number of such repeated hybridizations is often small. I therefore represent these values by their gene-wise median rather than their gene-wise average because the median is less sensitive to outliers. The need remains, though, to visualize also the original data and not only the median since they contain valuable information about experimental variance and quality of individual hybridizations. In fact, CA offers the possibility to reflect both aspects. To this end, CA is first effected by using the gene-wise medians, determining the coordinate system to embed the original hybridization intensities. These data points are then referred to as supplementary points or points without mass. Thus



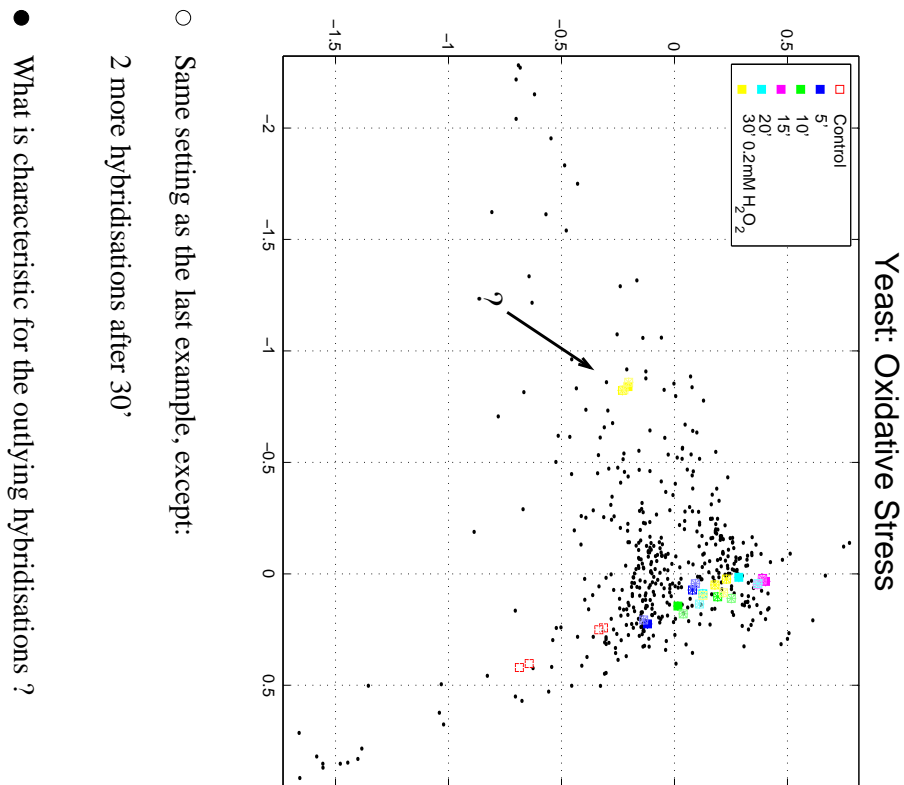
Due to all these precautions and given a sufficient number of repeated hybridizations, the variance explained by a CA plot will largely reflect biological changes, displaying the significance of differences both among the genes and among the hybridizations in terms of the χ^2 -statistic. The power of the CA technique however is that it is able to show associations between genes and hybridizations. To fully exploit this property, it is necessary to examine the exact directions of gene-association with the experimental conditions. These are given by the standard coordinates of the according condition medians rather than by their principle coordinates. An experiments represented in standard coordinates can be viewed as a virtual gene having its entire mass (intensity) in this particular experiment. Thus, it is the gene of highest possible association with this experiment, able to “represent” the experiment in “gene-space”. Plotting the standard coordinates directly would cause all principle coordinates to shrink into a small area in the middle of the plot. The introduction of lines representing the standard coordinates is of great help in the interpretation of the plots, relating genes and conditions to each other and circumventing direct plotting.

The biological context of CDC14 is sketched in the following transparency.



The last data example relates to the second part of the talk. A time course has been recorded for wild type *S. cerevisiae* cells under oxidative stress. The thin black arrow draws the chronological progression of the experiment. The cells responding to 0.2mM hydrogenperoxide in their medium show quite a leap in expression behaviour between 15 and 20 minutes that includes

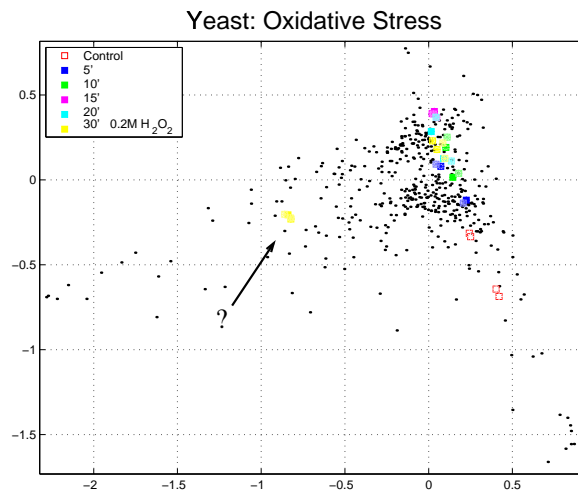
the downregulation of genes which had been switched on in the initial phase of the response. Four of those are flagged. Their gene profiles are plotted below. They are switched on initially and are being downregulated somewhere between 15 and 20 minutes.



- Same setting as the last example, except:
2 more hybridisations after 30'
- What is characteristic for the outlying hybridisations ?

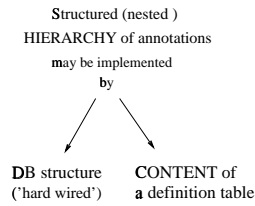
In the above example there is obviously something wrong. It is exactly the same experimental setting as before but now the yellow 30' condition is divided into two clusters located far away from each other and distorting the nice picture of the previous plot.

And we want to know why. What is wrong with the outliers? In other words: Can we find features in the experimental description which are characteristic for the outlying cluster? Are there annotation values overrepresented in the cluster? Or are there values missing or underrepresented in the cluster?



What is characteristic for the outlying hybridisations ?

In practise: Selecting these outliers, scanning for at least 2-fold over-or underrepresented annotation values results in values belonging to only 8 out of 111 annotations, listed in the next transparency.



Given the tool of a relational DBMS, storage of e.g. experiment annotations can be implemented in different ways.

by STRUCTURE

annotations stored as attributes
(= columns, fields)

experiment	array_source	array_support	spotted_material
1	self_made	nylon	PCR
2	genome_systems	polypropylene	PCR
3	self_made	glas	colonies
⋮			
⋮			

by CONTENT

... stored in table content

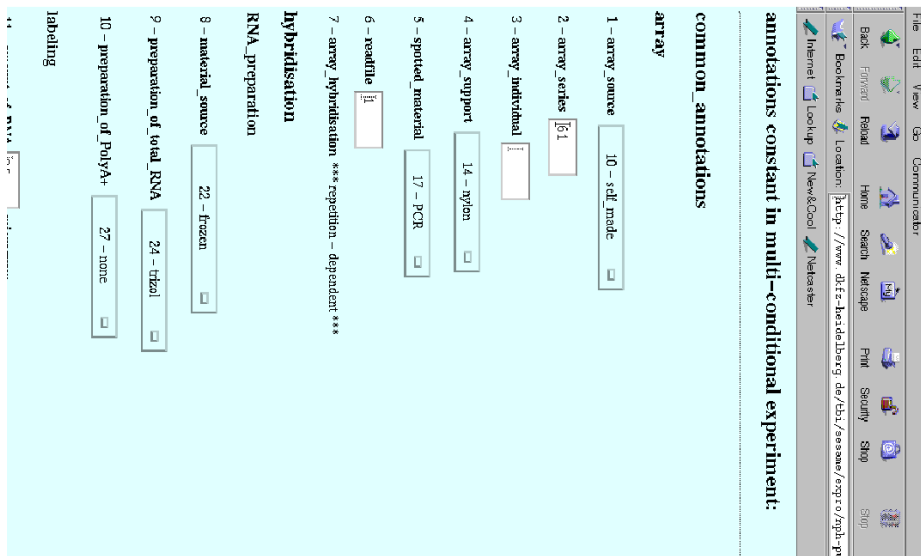
DEFINITIONS

annotation	defined value
array_source	self_made
array_source	genome_systems
array_support	glass
array_support	nylon
array_support	polypropylene
spotted_material	colonies
spotted_material	PCR

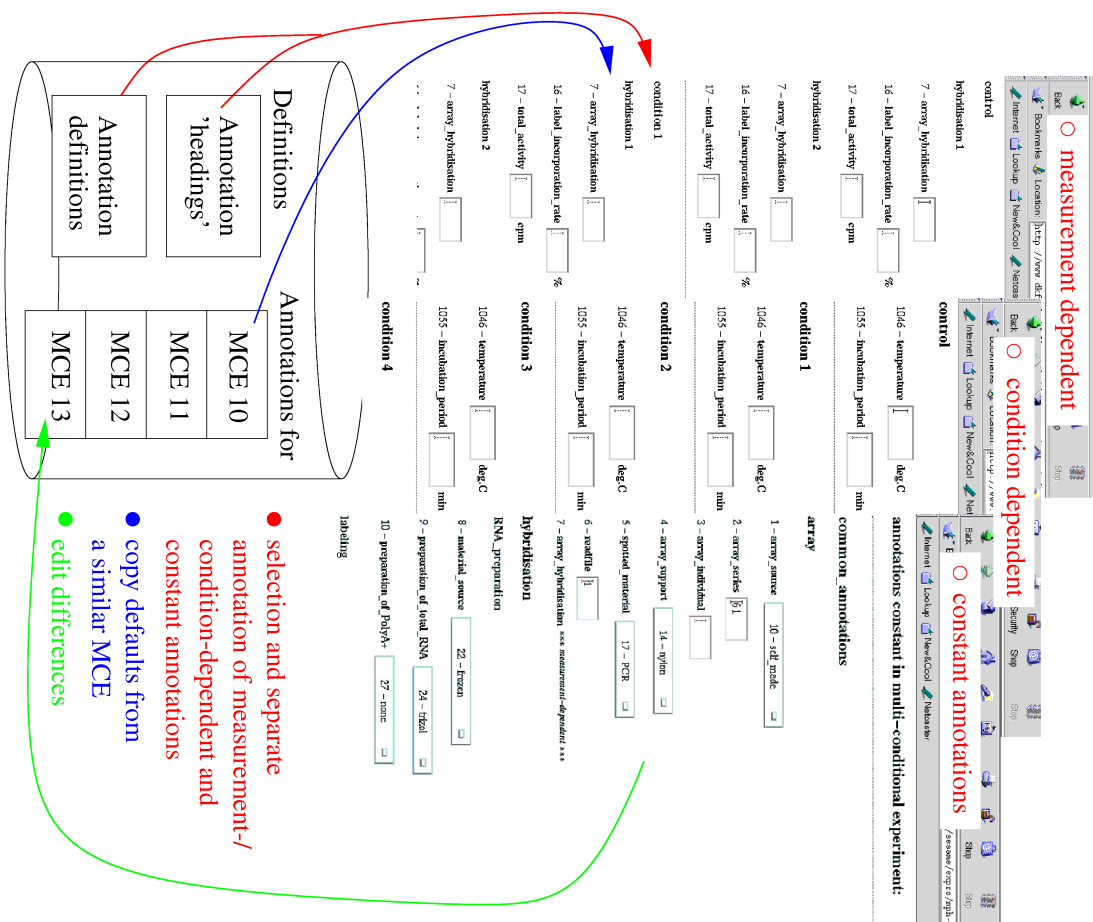
ANNOTATIONS

experiment	annotation	value
1	array_source	self_made
1	array_support	nylon
1	spotted_material	PCR
2	array_source	genome_systems
⋮		
⋮		

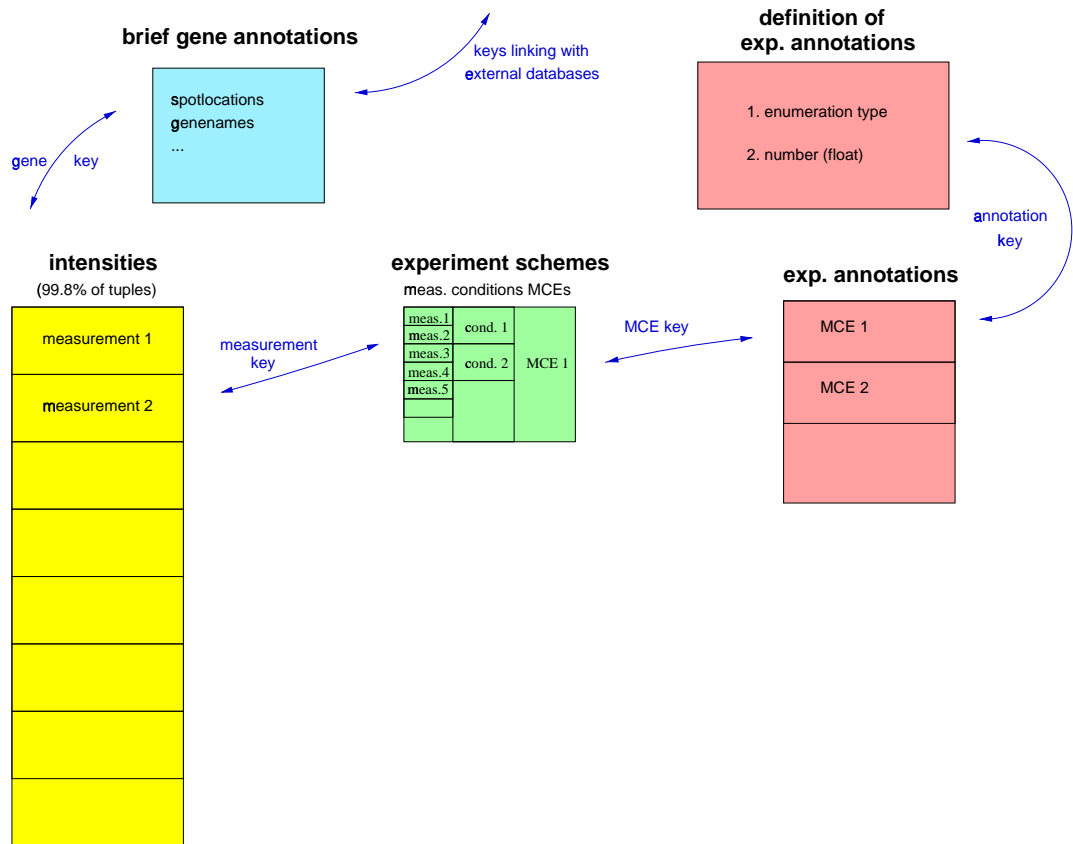
The parameter names such as “array source”, let us refer to them as “annotations”, may become the attributes (column names) of a single table. Another possibility is to make them the content (the tuples) of a first table, whose only purpose is to define the annotations along with the values they may take. Here, a second table is needed to store the actual values taken in particular experiments.



The content of these definition tables serves as meta data to compile html forms used during the process of annotating an experiment.



A convenient way minimizing efforts in annotation. Every piece of information has to be entered only once. The annotation process may start with copying default values from the most



Above transparency shows them (lower right boxes) in database context. Gene annotations, signal intensities (please note the percentage!), and experiment annotations are displayed in blue, yellow and red, respectively, also in the next transparency. The gene annotations are linked both with the transcription intensities and with public external gene databases (e.g. GO) in order to enable explicit characterization of genes showing a particular transcription behaviour. The intensities are stored as measurements. A measurement (i.e. a hybridization for radioactive or a single channel for multi-channel data) comprises a single value for each spot on the microarray. Experiment schemes record for each measurement which hybridization and experimental condition it belongs to, and which multiconditional experiment (MCE) this condition is contained in. The experiment schemes are the ‘storekeepers’ of the database, relating intensity data with experiment annotations, which allow for explicit characterization of measurements showing a particular expression pattern.

